

MULTIPLICATIVE λ -*-JORDAN TRIPLE HIGHER DERIVATIONS ON STANDARD OPERATOR ALGEBRAS

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Abstract. Let \mathcal{A} be a standard operator algebra on an infinite dimensional complex Hilbert space \mathcal{H} containing an identity operator \mathcal{I} . In this paper, it is shown that any multiplicative λ -*-Jordan triple higher derivation $\mathcal{D} = \{\delta_n\}_{n \in \mathbb{N}}$ from \mathcal{A} to $\mathcal{B}(\mathcal{H})$ is an additive *-higher derivation on \mathcal{A} . In particular, \mathcal{D} is inner.

Mathematics subject classification (2020): 47B47, 16W25, 46K15.

Keywords and phrases: Derivation, standard operator algebra, multiplicative λ -*-Jordan triple higher derivations.

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