

BILINEAR CALDERÓN–ZYGmund OPERATORS ON TWO WEIGHT HERZ SPACES WITH VARIABLE EXPONENTS

SHENGRONG WANG AND JINGSHI XU*

Abstract. In this paper, we obtain the boundedness of bilinear Calderón–Zygmund operators on two weight Herz spaces with variable exponents.

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