

ON JORDAN BIDERIVATIONS OF TRIANGULAR RINGS

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Abstract. The aim of the paper is to give a description of Jordan biderivations for a certain class of triangular rings. It is shown that, under some mild conditions, every Jordan biderivation of the triangular rings is a biderivation. The result is then applied to some upper triangular matrix rings.

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