LOCAL AND 2–LOCAL ISOMETRIES BETWEEN ABSOLUTELY CONTINUOUS FUNCTION SPACES

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Abstract. In this paper we give a complete description of local and 2-local isometries defined between spaces of scalar-valued absolutely continuous functions on arbitrary (not necessarily compact) subsets of the real line with at least two points.

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