

## REFINING AND REVERSING JENSEN'S INEQUALITY

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*Abstract.* This paper is focused on Jensen's inequality and its variants. Various refinements and reverses of Jensen's inequality, including scalar and operator versions, are given.

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