

SOLUTION ALGORITHM OF THE INVERSE SPECTRAL PROBLEM FOR DIRAC OPERATOR WITH A SPECTRAL PARAMETER IN THE BOUNDARY CONDITION

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Abstract. We consider an inverse problem for Dirac system in case where one of nonseparated boundary conditions involves a linear function of spectral parameter. We prove the uniqueness theorem for the solution of this problem and then, based on this theorem, we construct a solution algorithm for the considered problem.

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