

## COMPLEX SYMMETRIC WEIGHTED COMPOSITION–DIFFERENTIATION OPERATORS OF ORDER $n$ ON THE WEIGHTED BERGMAN SPACES

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*Abstract.* We study the complex symmetry of weighted composition–differentiation operators of order  $n$  on the weighted Bergman spaces  $A_{\alpha}^2$ . Several concrete examples are provided.

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