A CRITERION OF LOCAL DERIVATIONS ON THE SEVEN–DIMENSIONAL SIMPLE MALCEV ALGEBRA

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Abstract. In the present paper we give a matrix form of local derivations of the complex finite dimensional simple (non-Lie) Malcev algebra $\mathbb{M}$, and a direct proof of the statement that every 2-local derivation of $\mathbb{M}$ is a derivation. We have some description of local and 2-local derivations of complex finite-dimensional semisimple binary Lie algebras.

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