

A ROTATION OF WIENER INTEGRAL ASSOCIATED WITH BOUNDED OPERATORS ON ABSTRACT WIENER SPACES

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Abstract. In this paper, we establish a rotation theorem for the Wiener integral associated with bounded operator on abstract Wiener spaces. To do this, we introduce a class of the angle preserving operators defined on the abstract Wiener space B .

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