MEAN ERGODICITY OF MULTIPLICATION
OPERATORS ON THE BLOCH AND BESOV SPACES

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Abstract. In this paper, the power boundedness and mean ergodicity of multiplication operators are investigated on the Bloch space $\mathscr{B}$, the little Bloch space $\mathscr{B}_0$ and the Besov Space $\mathscr{B}_p$. We completely characterize power bounded, mean ergodic and uniformly mean ergodic multiplication operators on $\mathscr{B}$ and $\mathscr{B}_0$.

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