

NOTE ON BOUNDS FOR EIGENVALUES USING TRACES

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Abstract. Some extensions of the results related to bounds for the eigenvalues and spreads of matrices using traces are discussed here. We also obtain bounds for the eigenvalues of a positive definite matrix in terms of its trace and trace of its inverse.

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