THE STRONG LIMITED p–SCHUR PROPERTY IN BANACH LATTICES

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Abstract. The concept of the strong limited p-Schur property ($1 \leqslant p \leqslant \infty$); that is, spaces on which every weakly p-compact and almost limited set is relatively compact is introduced and studied. Next, the weak DP* property of order p is defined and spaces with this property are characterized. As an application of these results, by the class of disjoint p-convergent operators, some characterizations of Banach lattices with the weak DP* property of order p are given.

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