Operators and Matrices
Volume 16, Number 4 (2022), 1185–1189
doi:10.7153/oam-2022-16-77

THE DENSITY OF STATES DEPENDS ON THE DOMAIN

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Abstract. In this short note we demonstrate that the definition of the density of states of a Schrödinger operator with bounded potential in general depends on the choice of the domain undergoing the thermodynamic limit.

Mathematics subject classification (2020): 47N50, 35J10.
Keywords and phrases: The density of states, Schrodinger operator, radially homogeneous potential.

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Paper OaM-16-77