POSITIVE OPERATOR–VALUED TOEPLITZ OPERATORS
ON VECTOR–VALUED GENERALIZED FOCK SPACES

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Abstract. In this paper, we obtain several equivalent descriptions of Carleson conditions to characterize the boundedness and compactness of positive vector-valued Toeplitz operators on the vector-valued generalized Fock spaces $F_\varphi^p(\mathcal{H})$.

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