ON ANDO–HIAI TYPE INEQUALITIES FOR SECTORIAL MATRICES

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Abstract. In a recent paper of the same journal, Zhao, Zheng and Jiang generalized a norm inequality of Ando and Hiai for sectorial matrices. We first improve their main result by reducing the coefficient to a smaller one. We also present an analogous inequality involving the logarithmic mean.

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