

CORE INVERSE OF OPERATORS IN HILBERT SPACES

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Abstract. This article includes the core inverses of operators on Hilbert spaces. In addition, the group inverses and Moore-Penrose inverses of these operators are characterised.

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