

## AN ELEMENTARY PROOF OF A HLAWKA TYPE INEQUALITY

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*Abstract.* In this paper, we provided an elementary proof of a multiple Hlawka type inequality proved by W. Berndt and S. Sra in [1]. Our proof does not use the tensor product method.

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