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XY–CONVEX FREE POLYNOMIALS REVISITED

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Abstract. In this article, by using the matrix-valued analog of a factorization property of free polynomials, we offer an alternate approach to the structure of matrix-valued hermitian free polynomials that are xy-convex.

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