

A NEW OSCILLATORY CRITERION FOR THE GENERALIZED HILL'S EQUATION

G. A. GRIGORIAN

Abstract. In this note we use an oscillatory theorem for the second order linear ordinary differential equation in order to establish an oscillatory criterion for the generalized Hill's equation. We formulate a hypothesis about representation of the sum of periodic functions with rational dependent periods by a sum of periodic functions with rational independent periods.

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