

## ON THE STABILITY OF SYSTEMS OF TWO LINEAR FIRST-ORDER ORDINARY DIFFERENTIAL EQUATIONS

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*Abstract.* The Riccati equation method is used to establish some new stability criteria for systems of two linear first-order ordinary differential equations. It is shown that two of these criteria in the two dimensional case imply the Routh-Hurwitz's criterion.

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