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HOMOTOPY PERTURBATION METHOD TO FRACTIONAL BIOLOGICAL POPULATION EQUATION

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Abstract. In this paper, the Homotopy perturbation method is successfully extended to solve fractional biological population model and numerical results are obtained. The fractional derivatives are described in the Caputo sense, some examples are provided. And the solutions of the equation are continuous with the parameter α.

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