

## ON REFINEMENTS OF HERMITE–HADAMARD TYPE INEQUALITIES WITH GENERALIZED FRACTIONAL INTEGRAL OPERATORS

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**Abstract.** In this paper we establish the refinements of Hermite–Hadamard type inequalities for generalized fractional integral operator through the instrument of convex functions.

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