

GLOBAL SOLUTIONS OF ANOMALOUS DIFFUSION SYSTEMS 3×3

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Abstract. In this article, we establish a global existence result for a nonlinear reaction-diffusion system in the case of 3 components with fractional Laplacians. Our proof method is based on the well-known regularizing effect.

Mathematics subject classification (2020): 35K57, 37L05, 35A01, 35R11.

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