

ON TRIPLE SEQUENCE OF BERNSTEIN OPERATOR OF WEIGHTED ROUGH I_λ -CONVERGENCE

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Abstract. We introduce and study some basic properties of rough I_λ -convergence of weight g , where $g : \mathbb{N}^3 \rightarrow [0, \infty)$ is a function satisfying $g(m, n, k) \rightarrow \infty$ and $\frac{\|(m, n, k)\|}{g(m, n, k)} \not\rightarrow 0$ as $m, n, k \rightarrow \infty$, of triple sequence of Bernstein polynomials and also study the set of all rough I_λ -convergence of weight g limits of a triple sequence of Bernstein polynomials and relation between analyticness and rough I_λ -convergence of weight g of a triple sequences of Bernstein polynomials.

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