

STATISTICAL CONVERGENCE IN 2-METRIC SPACES

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Abstract. In this paper, notions of statistical convergence, statistically Cauchy sequence, \mathcal{N} - and lacunary statistical convergence in 2-metric space will be introduced. Also some inclusion relations between these concepts will be investigated.

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