

ON IDEAL CONVERGENCE OF NESTED SEQUENCES OF SETS

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Abstract. In this work, we show the equivalence of ideal Wijsman convergence and Wijsman convergence and the equivalence of ideal Hausdorff convergence and Hausdorff convergence for the nested sequences of sets. Then we prove that the ideal Wijsman limit and the ideal Hausdorff limit of the nested sequence of sets are equivalent each other for every admissible ideal.

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