

## ON CERTAIN NEW MODULAR RELATIONS FOR RAMANUJAN'S CONTINUED FRACTIONS OF SIXTEEN ORDER

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**Abstract.** In this paper, we derive several beautiful modular relations for the Ramanujan's continued fractions of sixteen order by using Ramanujan's theta functions.

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