

## DUALS OF PASCAL SEQUENCE SPACES VIA MODULUS FUNCTION

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**Abstract.** The main goal of this paper is to introduce the new concept of sequence spaces by using Pascal matrix via modulus function. We investigate various algebraic, topological properties and inclusion relation of the newly constructed sequence space. We also make and efforts to find duals of these spaces.

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