

## ON WEIGHTED ČEBYŠEV–GRÜSS TYPE INEQUALITIES ON TIME SCALES

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*Abstract.* In this study, we establish weighted Čebyšev–Grüss type inequalities on time scales.

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