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ESTIMATING THE NORMALIZED JENSEN FUNCTIONAL

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Abstract. We establish upper and lower bounds for the normalized Jensen functional in the context of $\left(M_{[\varphi]},A\right)$-convexity. In connection with these results, a refinement of the triangle inequality is proved.

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