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# BOUNDEDNESS FOR THE MULTI–COMMUTATORS OF CALDERÓN–ZYGMUND OPERATORS

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*Abstract.* In this paper, the authors study the multi-commutators $\mathscr{T}^{A_1,\cdots,A_k}$ generalized by the Calderón-Zygmund operator $T$ and the $(m_i+1)$-th remainders of Taylor series of the functions $A_i$ whose $m_i$-th derivatives belong to $BMO$ spaces for $m_i \geqslant 0$ and $i = 1,2,\cdots,k$. The boundedness from the weighted central Morrey space $B_p(w)$ to the weighted central $BMO$ space $CMO(w)$ for these multi-commutators was derived. As corollary, the $L^p$-boundedness for the multi-commutators has been obtained.

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