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MORE INEQUALITIES FOR POSITIVE LINEAR MAPS

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Abstract. We derive inequalities for the norm of the variance of matrices. It is shown that unital linear maps on 2×2 matrices preserve the commutativity properties of matrices. This feature allows us to generalize several inequalities for such maps. We show by way of an example that this technique cannot be extended to the case of $n \times n$, $n \geqslant 3$, matrices.

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