Journal of
Mathematical
Inequalities
Volume 7, Number 4 (2013), 617–645 doi:10.7153/jmi-07-58

NEW CONVERSES OF THE JESSEN AND LAH–RIBARIČ INEQUALITIES II

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Abstract. New converses of the Jessen and Lah-Ribarič inequalities for continuous convex functions are studied. Applications are given for generalized and arithmetic means, Hölder's inequality, Hadamard's inequality, and the inequalities of Giaccardi and Petrović.

Mathematics subject classification (2010): 26A51, 26E60, 97H30.
Keywords and phrases: Positive linear functionals, Jensen's inequality, Lah-Ribarič's inequality, convex functions, generalized means, arithmetic means, Hölder's inequality, Hadamard's inequality, inequalities of Giaccardi and Petrović.

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Paper JMI-07-58