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NONLINEAR DIFFERENCE INEQUALITIES WITH AN INFINITE SUMMATION AND THEIR APPLICATIONS

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Abstract. Some new infinite difference inequalities involving two independent variables with more than one nonlinear terms are established. These inequalities provide a handy tool in deriving the boundedness and uniqueness of solutions of certain nonlinear infinite difference equations.

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