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IMPROVED YOUNG AND HEINZ INEQUALITIES WITH THE KANTOROVICH CONSTANT

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Abstract. In this article, we study the further refinements and reverses of the Young and Heinz inequalities with the Kantorovich constant. These modified inequalities are used to establish corresponding operator inequalities on a Hilbert space and Hilbert-Schmidt norm inequalities.
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