

## APPROXIMATION OF QUADRATIC LIE $*$ -DERIVATIONS ON $\rho$ -COMPLETE CONVEX MODULAR ALGEBRAS

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**Abstract.** In this paper, we investigate stable approximation of almost quadratic Lie  $*$ -derivations associated with approximate quadratic mappings on  $\rho$ -complete convex modular algebras  $\chi_\rho$  by using  $\Delta_2$ -condition via convex modular  $\rho$ .

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