

FUZZY MEANS AND HGA-TYPE INEQUALITIES

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Abstract. The notion of fuzzy means of fuzzy numbers is introduced. Fuzzy counterparts of the arithmetic, geometric and harmonic means are investigated and inequalities between them are presented.

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