

VECTORIAL AND METRICAL RELATIONS IN TETRAHEDRON

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Abstract. The scope of this paper is twofold. On the one hand we will study some new vector relations in triangle and tetrahedron and on the other hand we will proof this relations not just for vector case but also in some special coordinates, more precisely in Wachpress's coordinates. The investigated results from this paper are done in order to find some new metric relations in triangle and tetrahedron.

Mathematics subject classification (2020): 51M20.

Keywords and phrases: Vectorial relations, metrical relations, tetrahedron.

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