

## ALMOST SURELY STABILITY OF DELAY HYBRID STOCHASTIC SYSTEM DRIVEN BY LÉVY NOISE

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*Abstract.* This study is devoted to investigate the almost sure stability of a class of nonlinear delay hybrid stochastic system driven by Lévy noise. We derive that the system has a unique global solution. Then, we discuss the almost sure stability of the stochastic system. A numerical example is provided to verify the results.

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