A NEW BOUND FOR THE FIRST EIGENVALUES OF
THE BIHARMONIC OPERATOR ON MANIFOLD

SHAHROUD AZAMI* AND MOHAMMAD JAVAD HABIBI VOSTA KOLAEI

Abstract. Consider (M^n, g) as a complete simply connected Riemannian manifold. Also let N^m for $m \leqslant n$ be a complete noncompact submanifold in M. In this paper, we are going to find a lower bound for the first eigenvalues of famous buckling and clamped plate problems on submanifold N with mean curvature H.

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