

## THE LINEAR CANONICAL HANKEL WAVELET TRANSFORM ON GELFAND–SHILOV SPACES

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**Abstract.** In this article, we discussed some fruitful estimates for linear canonical Hankel transform on some Gelfand-Shilov spaces of type  $W$ . Also boundedness result of wavelet transform involving the linear canonical Hankel transform on certain  $W$ -type spaces.

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