

STRONG DOUBLING CONDITIONS

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Abstract. We show that the class of strong doubling measures depends essentially on the parameter r , and that the measure of the boundary layer of a QHBC domain decays geometrically, if the measure is suitably strong doubling.

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