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SHORT PROOFS OF THE GALE & RYSER AND FORD & FULKERSON CHARACTERIZATIONS OF THE ROW AND COLUMN SUM VECTORS OF (0,1)–MATRICES

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Abstract. We simultaneously give short, direct proofs of the Gale & Ryser and Ford & Fulkerson characterizations of the row and column sum vectors of (0,1)-matrices.

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