

ON NEW PROOFS OF WILKER'S INEQUALITIES INVOLVING TRIGONOMETRIC FUNCTIONS

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Abstract. In the note, some new proofs for inequalities involving trigonometric functions are given.

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