

## A KALLMAN–ROTA INEQUALITY FOR EVOLUTION SEMIGROUPS

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*Abstract.* A Kallman-Rota type inequality for evolution semigroups and applications for real valued functions are given.

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