

## CONTROLLABILITY OF NONAUTONOMOUS SEMILINEAR INTEGRODIFFERENTIAL INCLUSIONS IN BANACH SPACES

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**Abstract.** In this paper, we establish a sufficient condition for the controllability of nonautonomous integrodifferential inclusions with nonlocal conditions in Banach spaces. The approach used is the Sadovskii's fixed point theorem with the theory of resolvent operators.

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