

SOME NEW OPIAL DYNAMIC INEQUALITIES WITH WEIGHTED FUNCTIONS ON TIME SCALES

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Abstract. In this paper we prove some new dynamic inequalities with two weight functions and some new dynamic inequalities with two unknown functions of Opial type on time scales. The main results will be proved by employing Hölder's inequality, the chain rule and some basic algebraic inequalities.

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