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ON THE COMPACTNESS OF THE STEVIĆ–SHARMA OPERATOR ON THE LOGARITHMIC BLOCH SPACES

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Abstract. Let $H(\mathbb{D})$ denote the space of all analytic functions on the unit disc $\mathbb{D}$ of the complex plane $\mathbb{C}$, $\psi_1, \psi_2 \in H(\mathbb{D})$, and φ be an analytic self-map of $\mathbb{D}$. In this paper, we characterize the compactness of the Stević-Sharma operator on the logarithmic Bloch spaces.

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