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ESSENTIAL NORM OF WEIGHTED COMPOSITION OPERATORS BETWEEN BLOCH–TYPE SPACES IN THE OPEN UNIT BALL

JUNTAO DU AND XIANGLING ZHU

Abstract. In this paper, we give an estimation for the essential norm of weighted composition operators between Bloch-type spaces in the open unit ball of $\mathbb{C}^n$.

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