Mathematical
Inequalities
& Applications
Volume 22, Number 3 (2019), 967–982 doi:10.7153/mia-2019-22-65

ESSENTIAL NORM OF THE WEIGHTED DIFFERENTIATION COMPOSITION OPERATOR BETWEEN BLOCH–TYPE SPACES

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Abstract. We give some characterizations for the boundedness and compactness of weighted differentiation composition operator $D^n_{\varphi,u}$ between different Bloch spaces, and also estimate the essential norms of the operator, complementing some recent results in the literature.

Mathematics subject classification (2010): 47B38, 30H30, 30H05, 47B33.
Keywords and phrases: Weighted differentiation composition operator, essential norm, Bloch-type space, boundedness, compactness.

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Paper MIA-22-65

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